

# Multi-objective Hybrid Optimal Control for Interplanetary Mission Planning

5

0

5



Jacob Englander 4-1-2015 **(1)** 

O

0

C

NAVIGATION & MISSION DESIGN BRANCH NASA GSFC



www.nasa.gov

#### The Team

- NASA Goddard Space Flight Center
  - Jacob Englander
  - Frank Vaughn
- a.i. solutions
  - Matthew Vavrina
- University of Illinois
  - Professor Bruce Conway
  - Dr. Alexander Ghosh
  - Donald Ellison
  - Ryne Beeson
- University of Vermont
  - David Hinckley

# Introduction to the General Interplanetary Mission Design Problem

- The interplanetary design problem is composed of both discrete and real-valued decision parameters:
  - Choice of destination(s), number of planetary flybys, identities of flyby planets
  - Launch date, flight time(s), epochs of maneuvers, control history, flyby altitudes, etc.
- For example, for a main-belt asteroid mission, the designer must choose:
  - The optimal asteroid from a set of scientifically interesting bodies provided by the customer
  - Whether or not to perform planetary flybys on the way to the main belt and, if so, at which planets
  - Optimal trajectory from the Earth to the chosen asteroid by way of the chosen flyby planets

## **Unique Characteristics of Low-Thrust** Interplanetary Mission Design

- Low-thrust electric propulsion is characterized by high power requirements but also very high specific impulse (I<sub>sp</sub>), leading to very good mass fractions
- Low-thrust trajectory design is a very different process from chemical trajectory design
  - Chemical thrusters fire for minutes during a mission time-scale of years
    - Chemical maneuvers may be approximated as occurring instantaneously (impulsively)
    - This allows a mission designer to parameterize the cost of a chemical mission in units of "change in velocity," or Δv
    - Δv is invariant to changes in spacecraft hardware or launch vehicle, and mass fraction may be computed using only  $I_{sp}$  and  $\Delta v$
  - Electric thrusters fire for months or years, sometimes the entire mission duration
    - The mission designer therefore must choose a time-history of thrust control rather than discrete maneuvers
    - The impulsive approximation does not apply, and so the affect of the thruster must be continuously integrated as the spacecraft flies
    - The propellant flow rate required to provide a given thrust is dependent on the available power at that instant
    - Therefore different choices of power and thruster systems change the trajectory solution!

# Traditional Methods of Low-Thrust, Multi-Flyby Trajectory Design

- Several methods of picking the destination and flyby sequence:
  - Grid search over all possible choices of destinations, flyby sequence, propulsion system, power system, etc. (very expensive and often impractical)
  - Intuition-guided manual design of the trajectory (even more expensive, can miss non-intuitive solutions)
- Several methods of designing the trajectory:
  - Local optimization from an initial guess provided by a chemical mission design (but sometimes the optimal chemical trajectory does not resemble the optimal low-thrust trajectory)
  - Local optimization from an initial guess provided by a low-fidelity approximation to the low-thrust model, i.e. shaped-based methods (but sometimes the shape-based method cannot accurately approximate the true trajectory)

# **Brief History of Automated Interplanetary Trajectory Design**

- Gage, Braun, and Kroo, 1994 autonomous chemical design with variable mission sequence (no deep-space maneuvers)
- Vasile and de Pascale, 2005 autonomous chemical design for fixed mission sequence
- Vinko and Izzo, 2008 autonomous chemical design for fixed mission sequence
- Wall and Conway, 2009 autonomous low-thrust design for fixed mission sequence (no planetary flybys)
- Chilan and Conway, 2009 autonomous low-thrust and chemical design for fixed mission sequence (no planetary flybys)
- Yam, di Lorenzo, and Izzo, 2011 autonomous low-thrust design for fixed mission sequence
- Abdelkhalik and Gad, 2011, 2012, and 2013 autonomous chemical design with variable mission sequence
- Englander, Conway, and Williams, 2012 autonomous chemical design with variable mission sequence
- Englander (dissertation) 2013 autonomous low-thrust design with variable mission sequence

### **Automated Mission Design via Hybrid Optimal Control**

- Break the mission design problem into two stages, or "loops"
  - "outer-loop" picks sets of destinations, planetary flybys, sizes the power system, can pick propulsion system – a <u>discrete</u> optimization problem
  - "inner-loop" finds the optimal trajectory for a given candidate outerloop solution – a <u>real-valued</u> optimization problem
  - For the outer-loop to work, the inner-loop must function autonomously (i.e. no human interaction)

### Multi-Objective Hybrid Optimal Control

- The customer (scientist or project manager) most often does not want just one point solution to the mission design problem
- Instead, an exploration of a multi-objective trade space is required
- For a typical main-belt asteroid mission the customer might wish to see the trade-space of:
  - Launch date vs.
  - Flight time vs
  - Deliverable mass
  - While varying the destination asteroid, planetary flybys, solar array size, etc
- To address this question we use a multi-objective discrete outer-loop which defines many single objective real-valued inner-loop problems

#### **Outer-Loop Transcription and Optimization**

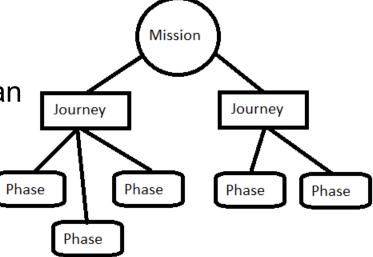
- The outer-loop finds the non-dominated trade surface between any set of objective functions chosen by the user
- Non-dominated surface means "no point on the surface is superior to any other point on the surface in all of the objective functions"
- The outer-loop solver may choose from a menu of options for each decision variable
- The choices made by the outer-loop solver are used to define trajectory optimization problems to be solved by the inner-loop

### **Anatomy of a Mission**

Break mission into a set of "journeys," each of which in turn is broken into "phases"

The endpoints of a journey are chosen in the problem assumptions

The endpoints of a phase (i.e. a flyby target) may be chosen by the user or an Outer-Loop solver



# **Outer-Loop Transcription: An Example**

<b>Asteroid Choices</b>	
Code	Body
0	Ceres
1	Pallas
2	Juno
3	Vesta
4	Astraea
5	Hebe
6	Iris
7	Flora
8	Metis
9	Hygiea
10	Parthenope
11	Victoria
12	Egeria
13	Irene
14	Eunomia
15	Psyche
16	Thetis

Flight time upper bound		
Code	Flight Time (y)	
0	6	
1	6.5	
2	7	
3	7.5	
4	8	
5	8.5	
6	9	
7	9.5	
8	10	
9	10.5	
10	11	
11	11.5	
12	12	
	Code 0 1 2 3 4 5 6 7 8 9 10 11	

Array Size		
Code	Power (kW)	
0	10	
1	11	
2	12	
3	13	
4	14	
5	15	
6	16	
7	17	
8	18	
9	19	
10	20	

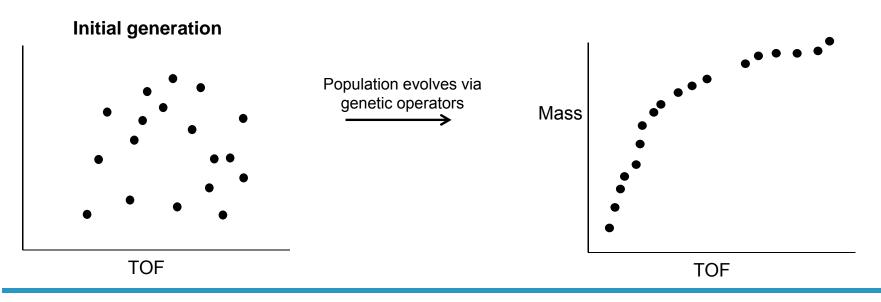
Flyby Choices (Journey 1)		
Code	Body	
0	Earth	
1	Mars	
2	none	
3	none	

lyby Choices (Journey 2)		
Code Body		
0	Mars	
1	none	

Sample Mission						
	Array Size	Flight Time Upper Bound	Asteroid 1	Potential Planetary Flyby 1	Asteroid 2	Potential Planetary Flyby 2
Code	8	4	0	1	1	1
Translation	18 kW	8 y	Ceres	Mars	Pallas	none

### Multi-Objective Optimization via NSGA-II

- The outer-loop optimization problem is solved using a discrete multiobjective solver, in this case Non-Dominated Sorting Genetic Algorithm II (NSGA-II)
- NSGA-II finds the non-dominated front, surface, or hyper-surface between any number of objectives chosen by the user

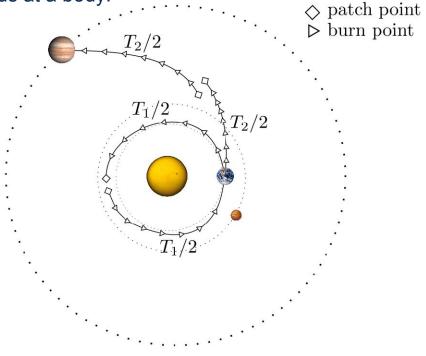


### Inner-Loop Modeling and Optimization

- The inner-loop solves a real-valued trajectory optimization problem which is defined by each candidate solution to the outer-loop problem
- The inner-loop must function autonomously because the problems are generated in real time and there is no opportunity for human intervention
- The outer-loop is only as good as the solutions to the inner-loop problem, so the inner-loop must be robust
- A given run of the outer-loop may require hundreds or even thousands of runs of the inner-loop, so the inner-loop must be fast
- If the individual inner-loop runs are independent then many of them can be run in parallel

### **Multiple Gravity Assist with Low-Thrust** (MGALT) via the Sims-Flanagan Transcription

- Break mission into phases. Each phase starts and ends at a body.
- Sims-Flanagan Transcription
  - Break phases into time steps
  - Insert a small impulse in the center of each time step, with bounded magnitude
  - Optimizer Chooses:
    - Launch date
      - For each phase:
        - Initial velocity vector
        - Flight time
        - Thrust-impulse vector at each time step
        - Mass at the end of the phase
        - Terminal velocity vector
- Assume two-body force model; propagate by solving Kepler's problem
- Propagate forward and backward from phase endpoints to a "match point"
- Enforce nonlinear state continuity constraints at match point
- Enforce nonlinear velocity magnitude and altitude constraints at flyby



## Power, Propulsion, and Ephemeris Modeling

- Medium-fidelity mission design requires accurate hardware modeling
- Launch vehicles are modeled using a polynomial fit

$$m_{delivered} = (1 - \sigma_{LV}) \left( a_{LV} C_3^5 + b_{LV} C_3^4 + c_{LV} C_3^3 + d_{LV} C_3^2 + e_{LV} C_3 + f_{LV} \right)$$

where  $\sigma_{LV}$  is launch vehicle margin and  $C_3$  is hyperbolic excess velocity

Thrusters are modeled using either a polynomial fit to published thrust and mass flow rate data

$$\dot{m} = a_F P^4 + b_F P^3 + c_F P^2 + d_F P + e_F$$
 $T = a_T P^4 + b_T P^3 + c_T P^2 + d_T P + e_T$ 

or, when detailed performance data is unavailable

$$T = \frac{2 \eta P}{I_{sp} g_0}$$

Power is modeled by a standard polynomial model

$$\frac{P_0}{r^2} \left( \frac{\gamma_0 + \frac{\gamma_1}{r} + \frac{\gamma_2}{r^2}}{1 + \gamma_3 r + \gamma_4 r^2} \right) (1 - \tau)^t$$

where  $P_0$  is the power at beginning of life at 1 AU and  $\tau$  is the solar array degradation constant

Ephemeris data for solar system bodies is provided via the SPICE toolkit

# Inner-Loop Solver: Nonlinear Programming (NLP)

Minimize 
$$f(x)$$
  
Subject to:  
 $x_{lb} \le x \le x_{ub}$   
 $c(x) \le 0$   
 $Ax \le 0$ 

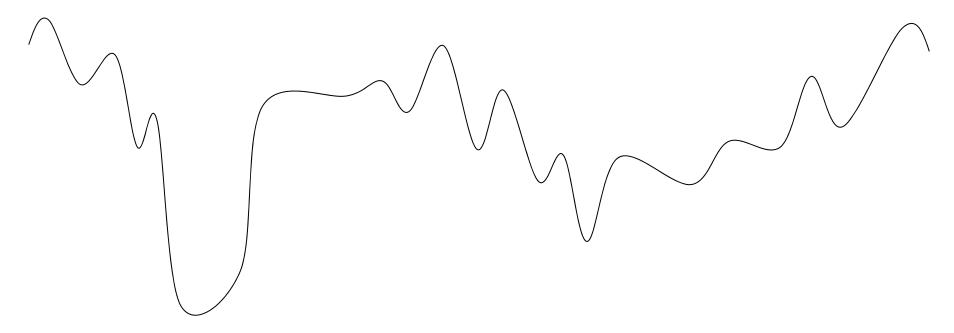
where:

 $x_{lb}$ ,  $x_{ub}$  are lower and upper bounds on the decision variables c(x) is a vector of nonlinear constraints

Ax is a vector of linear constraints

- There are several third party solvers that do this (SNOPT, IPOPT, fmincon, vf13AD)
- But all of these methods require an initial guess...

# Inner-Loop Solver: Monotonic Basin Hopping (MBH)



Leary, 2000 Vasile, Minisci, and Locatelli, 2009 Yam, di Lorenzo, and Izzo, 2011 Englander (dissertation), 2013 Casioli *et al.*, 2013 Englander and Englander, 2014 Improved from standard MBH by:

- 1. "Feasible point finder" aggregate penalty method
- 2. Non-uniform (Pareto) perturbation step
- 3. "Time-hop" operator (Casioli et al.)

# **Example: Main-Belt Two Asteroid Tour**

Mission Objective	it two main-belt asteroids with diameter greater than 50 km	
	(475 bodies meet this filter)	
Launch Vehicle	Atlas V 401	
Power System		
Array power at 1 AU	15 kW	
Cell performance model	1/r <sup>2</sup>	
Spacecraft bus power	800 W	
Power margin	15%	
Propulsion System		
Thruster	NEXT (throttle table 11, high-lsp mode)	
Number of thrusters	1	
Duty cycle	90%	
Propellant tank	unconstrained	
Mission Sequence up to two planetary flybys are permitted before the first asteroic		
	one between the first and second asteroids	
Inner-Loop Objective Function	Maximize delivered mass to second asteroid	
Outer-Loop Objective Functions Delivered mass to second asteroid		
	Launch year	
	Flight time	

# Main-Belt Two Asteroid Tour: Outer-Loop Menu

Launch Year		
Code	Year	
0	2020	
1	2021	
2	2022	
3	2023	
4	2024	
6	2025	
7	2026	
8	2027	
9	2028	
10	2029	

Flight Time Upper Bound		
Code	# Years	
0	5	
1	6	
2	7	
3	8	
4	9	
5	10	
7	11	
8	12	

First Asteroid		
Code	Body	
0	Ceres	
1	Pallas	
2	Juno	
3	Vesta	
4	Astraea	
5	Hebe	
6	Iris	
7	Flora	
	(475	
	choices)	

Second Asteroid		
Code	Body	
0	Ceres	
1	Pallas	
2	Juno	
3	Vesta	
4	Astraea	
5	Hebe	
6	Iris	
7	Flora	
	(475	
	choices)	

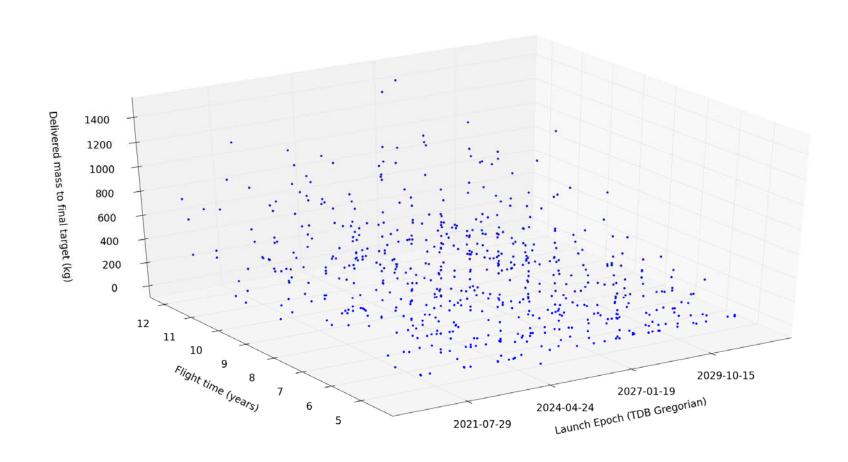
First Journey First Flyby		
Code	Body	
0	Earth	
1	Mars	
2	Jupiter	
3	No flyby	
4	No flyby	
5	No flyby	

First Journey Second Flyby		
Code	Body	
0	Earth	
1	Mars	
2	Jupiter	
3	No flyby	
4	No flyby	
5	No flyby	

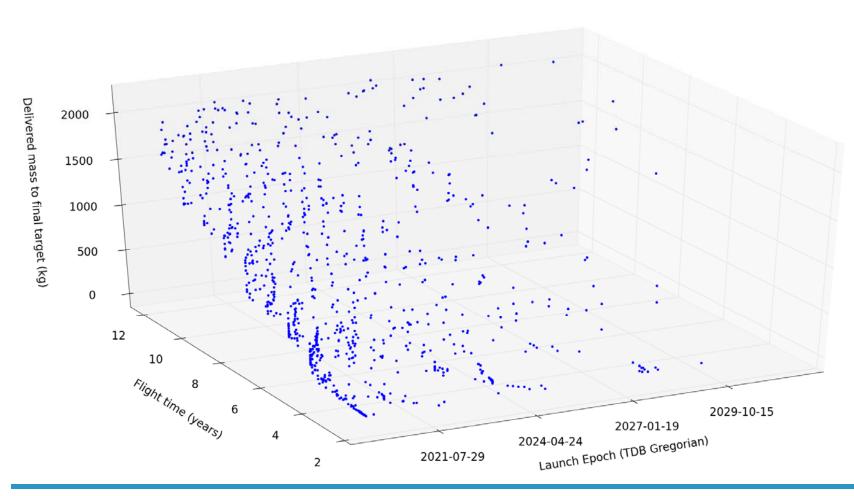
Second Journey Flyby	
Code	Body
0	Earth
1	Mars
2	Jupiter
3	No flyby
4	No flyby
5	No flyby

1.16x10<sup>9</sup>
possible
combinations,
4.82x10<sup>9</sup> with
duplicates

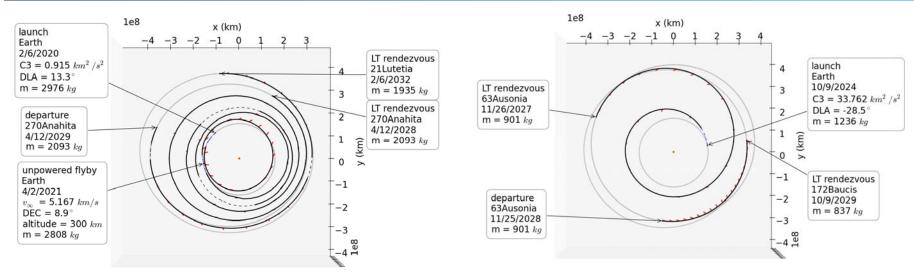
# **Main-Belt Two Asteroid Tour:** First Generation Trade Space



# Main-Belt Two Asteroid Tour: Final Generation Trade Space



# Main-Belt Two Asteroid Tour: Example Trajectories



A 12-year mission to Anahita and Lutetia delivers a very large science payload

A 5-year mission to Ausonia and Baucis delivers a smaller payload in less time and at a lower cost

Both of these candidate missions, and many others, would be valuable data points for our scientist customers

#### **Example: Deimos Large-Mass Sample Return**

Mission Objective	Return a large boulder from Deimos	
Launch Vehicle	Delta IV Heavy with lunar flyby (C3 2.0)	
Power System		
Array power at 1 AU	chosen by optimizer	
Cell performance model	1/r <sup>2</sup>	
Spacecraft bus power	2.0 kW	
Power margin	0%	
Propulsion System		
Thruster	chosen by optimizer (high-lsp or high-thrust versions of a large Hall	
	thruster)	
Number of thrusters	chosen by optimizer (3, 4, 5, or 6)	
Duty cycle	90%	
Propellant tank	unconstrained	
Mission Sequence	Direct travel to Mars followed by direct return to C3 2.0 for lunar flyby	
	capture	
	Mars arrival/departure is modeled using an Edelbaum spiral	
Inner-Loop Objective Function	Maximize sample return mass	
<b>Outer-Loop Objective Functions</b>	ective Functions Sample return mass	
	Solar array size	
	Launch epoch	
	Flight time	

# Deimos Sample Return: Outer-Loop Menu

Power Supply at 1 A	
Code	Array Outpu
0	40
1	41
2	42
3	43
4	44
5	45
6	46
7	47
8	48
9	49
10	50
11	51
12	52
13	54
14	56
15	58
16	60
17	62
18	64
19	66
20	68
21	70

Ī	Launch Year		
	Code	Year	
	0	2019	
	1	2020	
	2	2021	
	3	2022	
	4	2023	
	6	2024	
	7	2025	
	8	2026	
	9	2027	

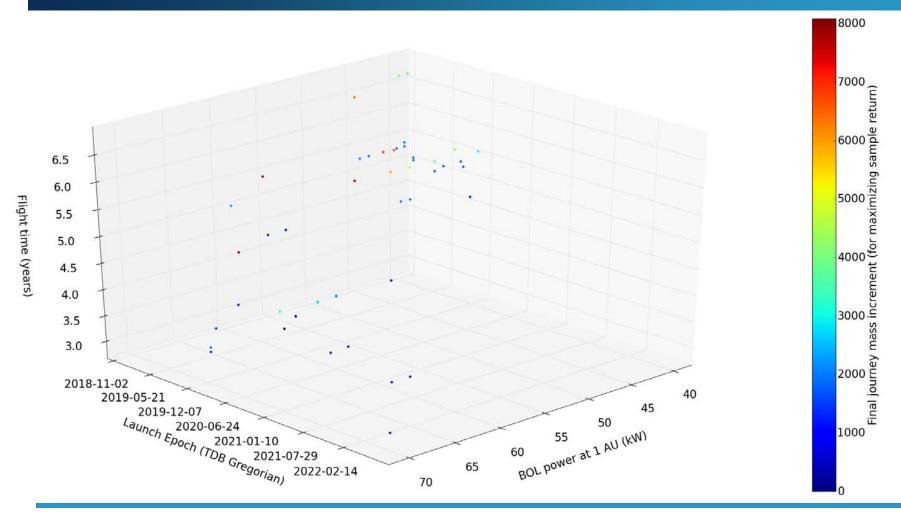
Flight Time	Upper Bound
Code	Days
0	800
1	900
2	1000
3	1100
4	1200
5	1300
7	1400
8	1500
9	1600
10	1700
26	3300

Thruster Type		
Code	Thruster	
0	13 kW Hall (High-Isp)	
1	13 kW Hall (medium-thrust)	
2	13 kW Hall (High-thrust)	

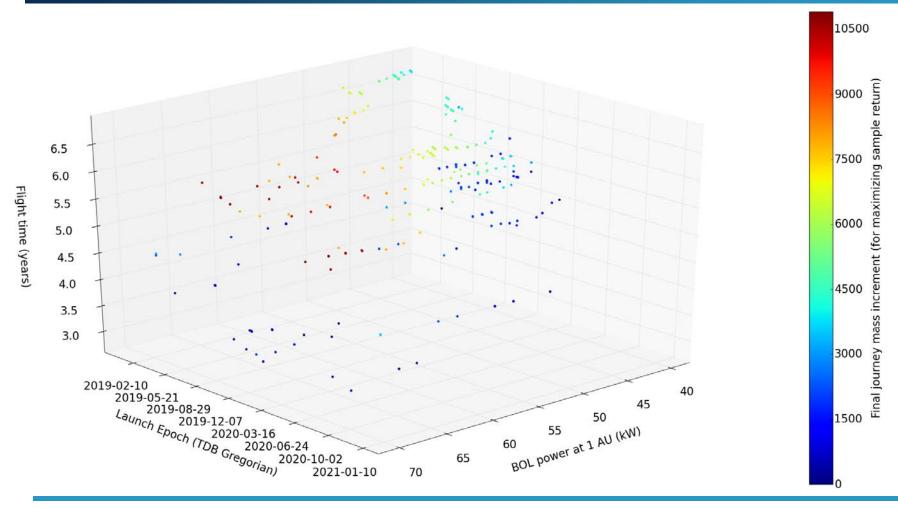
Number of Thrusters		
Code # Thrusters		
0	3	
1	4	
2	5	
3	6	

71280 possible combinations

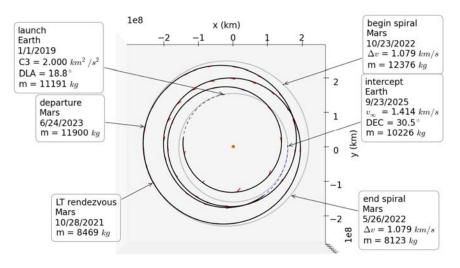
# **Deimos Sample Return: First Generation Trade Space**



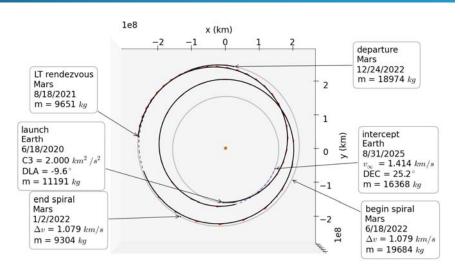
# Deimos Sample Return: Final Generation Trade Space



## Deimos Sample Return: Two Trajectories



A 7-year mission with a 41 kW solar array returns a 4 ton boulder



A 5-year mission with a 68 kW solar array returns a 10 ton boulder

Both of these candidate missions, and many others, would be of interest to our customers

#### **Conclusions**

- The low-thrust interplanetary mission and systems design problem may be posed as a multiobjective hybrid optimal control problem
- The combination of a multi-objective discrete NSGA-II outer-loop with a MBH+NLP inner-loop is a very powerful way to explore a mission and systems trade space in an efficient, automated manner
- The algorithm described here has revolutionized the low-thrust interplanetary mission design. process at NASA Goddard Space Flight Center
  - We can now study multiple mission design cases simultaneously, limited only by available computing power
  - Mission design engineers can now spend more time with the customer and with spacecraft hardware engineers so that we can fully understand the scientific and engineering context of our work
  - Good mission ideas are much less likely to be rejected due to lack of time to work on mission design, and bad ideas are much more likely to be rejected before they consume too many resources
- Skilled analysts are expensive. With a multi-objective HOCP automaton, analysts can focus on understanding the customer's needs and the spacecraft's capabilities and also detailed design work, leaving repetitive tasks to the computer

#### Thank you to our backers:

- NASA Goddard Space Flight Center Independent Research and Development (IRAD) program
- NASA Goddard Space Science Mission Operations (SSMO)
- NASA Graduate Student Researchers Program (GSRP)
- Illinois Space Grant
- Various customers at Goddard

#### **Thank You**

#### EMTG is available open-source at

https://sourceforge.net/projects/emtg/



# **Backup – Tuning Monotonic Basin Hopping**

## **Tuning Monotonic Basin Hopping (MBH)**

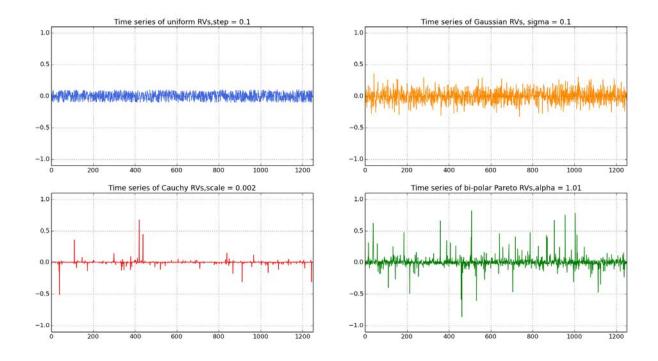
- We examined two components of classical MBH:
  - the random hops are driven by a uniform probability distribution; hops can occur in a ball of some user-defined radius about the current best point
  - There is a concept of "impatience" a certain number of iterations where the solution does not improve, after which the algorithm resets
- In this work we consider:
  - Alternative probability distributions (Gaussian, Cauchy, Pareto) which have the ability to "hop" over the entire solution space
  - Given the above, that the concept of "impatience" may not be necessary when using alternative probability distributions
- Our objective was to find a version of MBH that would be:
  - Efficient (find better solutions in less time)
  - Robust (work well on highly constrained problems and not be sensitive to tuning parameters)

#### **Probability Distributions and Their Tuning Parameters**

Distribution	RV Generator	Excursion Parameter
Uniform	$2\rho(r - 0.5)$	ho: ball size, impatience
Gaussian	$\frac{s}{\sigma\sqrt{2\pi}}e^{-\frac{r^2}{2\sigma^2}}$	$\sigma$ : standard deviation
Cauchy	$ \rho \tan (\pi (r - 0.5)) $	$\rho$ : scale
Pareto	$\frac{s}{\epsilon} \frac{(\alpha - 1.0)}{\left(\frac{\epsilon}{\epsilon + r}\right)^{-\alpha}}$	α: "parameter"

r = uniform(0.0,1.0), s is a fair coin flip,  $\epsilon = 1.0 * 10^{-13}$ 

#### **RV Generators**

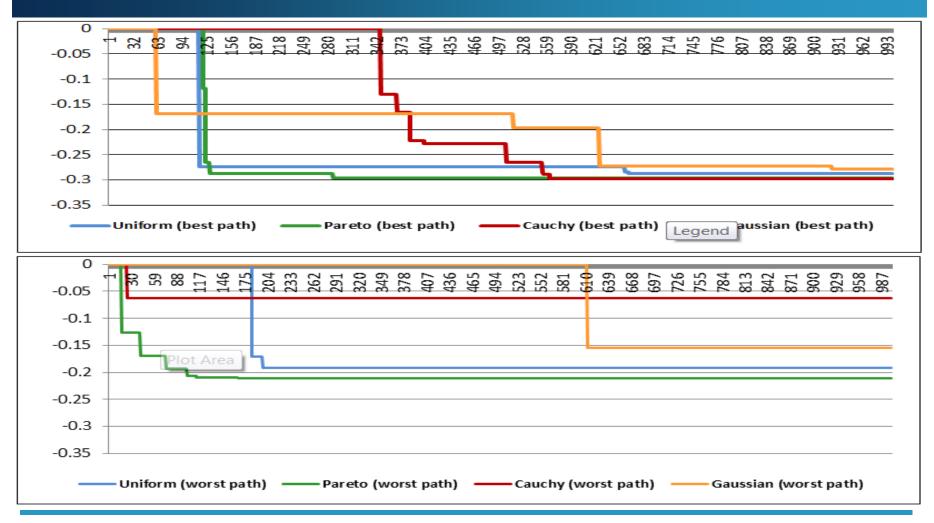


We want a distribution which takes lots of small steps to "exploit" the local region but also takes frequent large steps to "explore" the rest of the space.

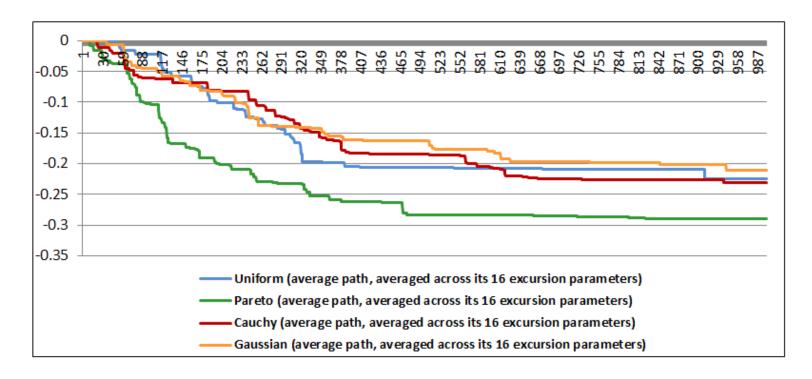
#### The Experiment

- 16 four-day (10000 step) runs of EMTG were conducted for each distribution
- Each of the 16 runs had a different value of the excursion parameter
- Impatience was turned off, i.e. MBH was never allowed to reset during the experiment
  - This was necessary to see how effectively each distribution could random-walk around the decision space

#### Results - Best and Worst Path



### Results – Average Performance



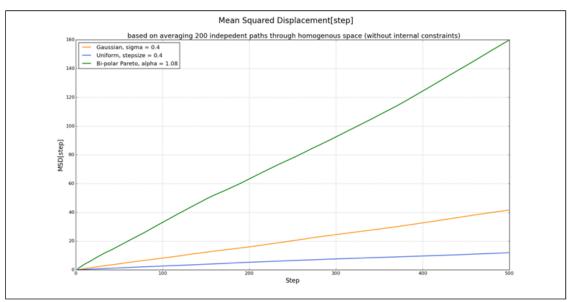
Pareto-driven MBH is most efficent (better solution in less time) and most robust (insensitive to tuning parameters)

### Why?

- Random walks (RWs) can be compared in terms of mean squared displacement (MSD)
  - A higher MSD means that an RW travels the problem space faster and more thoroughly than a lower MSD
- MSD can be used to describe RWs as diffusions through media
- In diffusion through homogeneous media (i.e. unconstrained problem spaces), RWs driven by independent identically distributed (i.i.d.) distributions with finite variance are considered "normally diffusive"
  - MSD proportional to the number of steps
- RWs driven by i.i.d. distributions with infinite variance are "super-diffusive"
  - MSD proportional to the number of steps raised to some power

#### Why? Continued....

- In a simplified test problem the Pareto RW is super-diffusive while the uniform and Gaussian RWs are normally diffusive (or just barely superdiffusive for Gaussian)
- It is difficult to plot MSD of the Cauchy RW on the same graph because Cauchy distributions do not have a mean



#### What about constraints?

- Constraints introduce serial negative auto-correlations
  - Constraint effectively restricts RW from moving in a certain direction, i.e. into the constraint
- Stochastic global search in constrained problem spaces can be described as diffusions through in-homogenous media
- When constraints are added to the simplified test problem, the uniform and Gaussian RWs become sub-diffusive but the Pareto distribution is still super-diffusive

